



The Federation of Middleham (VA) and Spennithorne (VC) CE Primary Schools

Executive Headteacher – Mrs Marie Mann

Blessed is the one who trusts in the Lord, whose confidence is in him.
 They will be like a tree planted by the water that sends out its roots by the stream.
 It does not fear when heat comes; its leaves are always green.
 It has no worries in a year of drought and never fails to bear fruit.

Jeremiah 17: 7 - 8

A PLACE TO LEARN, LOVE & GROW

Calculation Policy UPPER KEY STAGE 2: Year 5 & 6

In upper Key Stage 2, children build on secure foundations in calculation, and develop fluency, accuracy and flexibility in their approach to the four operations. They work with whole numbers and adapt their skills to work with decimals, and they continue to develop their ability to select appropriate, accurate and efficient operations.

Key language: decimal, column methods, exchange, partition, mental method, ten thousand, hundred thousand, million, factor, multiple, prime number, square number, cube number

Addition and subtraction: Children build on their column methods to add and subtract numbers with up to seven digits, and they adapt the methods to calculate efficiently and effectively with decimals, ensuring understanding of place value at every stage.
 Children compare and contrast methods, and they select mental methods or jottings where appropriate and where these are more likely to be efficient or accurate when compared with formal column methods.
 Bar models are used to represent the calculations required to solve problems and may indicate where efficient methods can be chosen.

Multiplication and division: Building on their understanding, children develop methods to multiply up to 4-digit numbers by single-digit and 2-digit numbers.
 Children develop column methods with an understanding of place value, and they continue to use the key skill of unitising to multiply and divide by 10, 100 and 1,000.
 Written division methods are introduced and adapted for division by single-digit and 2-digit numbers and are understood alongside the area model and place value. In Year 6, children develop a secure understanding of how division is related to fractions.
 Multiplication and division of decimals are also introduced and refined in Year 6.

Fractions: Children find fractions of amounts, multiply a fraction by a whole number and by another fraction, divide a fraction by a whole number, and add and subtract fractions with different denominators. Children become more confident working with improper fractions and mixed numbers and can calculate with them.
 Understanding of decimals with up to 3 decimal places is built through place value and as fractions, and children calculate with decimals in the context of measure as well as in pure arithmetic.
 Children develop an understanding of percentages in relation to hundredths, and they understand how to work with common percentages: 50%, 25%, 10% and 1%.

Year 5

Concrete

Pictorial

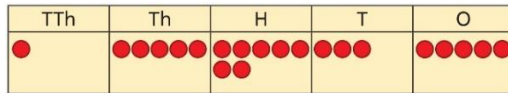
Abstract

Year 5
Addition

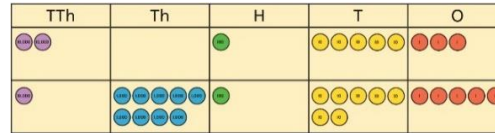
Column addition with whole numbers

Use place value equipment to represent additions.

Add a row of counters onto the place value grid to show $15,735 + 4,012$.



Represent additions, using place value equipment on a place value grid alongside written methods.



I need to exchange 10 tens for a 100.

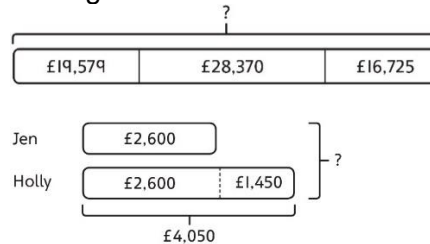
$$\begin{array}{r} \text{TTh Th H T O} \\ 20 \quad | \quad 53 \\ + 19 \quad | \quad 75 \\ \hline 39 \quad | \quad 28 \end{array}$$

Use column addition, including exchanges.

$$\begin{array}{r} \text{TTh Th H T O} \\ 19 \quad | \quad 75 \\ + 18 \quad | \quad 47 \\ \hline 37 \quad | \quad 92 \end{array}$$

Representing additions

Bar models represent addition of two or more numbers in the context of problem solving.



$$\begin{array}{r} \text{Th H T O} \\ 2600 \\ + 1450 \\ \hline 4050 \end{array} \quad \begin{array}{r} \text{Th H T O} \\ 2600 \\ + 4050 \\ \hline 6650 \end{array}$$

Use approximation to check whether answers are reasonable.

$$\begin{array}{r} \text{TTh Th H T O} \\ 23405 \\ + 7892 \\ \hline 20297 \end{array} \quad \begin{array}{r} \text{TTh Th H T O} \\ 23405 \\ + 7892 \\ \hline 31297 \end{array}$$

I will use $23,000 + 8,000$ to check.

Adding tenths

Link measure with addition of decimals.

Two lengths of fencing are 0.6 m and 0.2 m.
How long are they when added together?

Use a bar model with a number line to add tenths.

Understand the link with adding fractions.

$$\frac{6}{10} + \frac{2}{10} = \frac{8}{10}$$

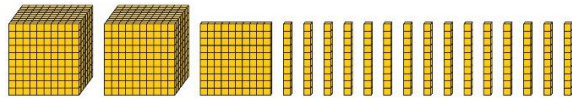
6 tenths + 2 tenths = 8 tenths

| | | |
|--|--|-------------------|
| | | $0.6 + 0.2 = 0.8$ |
|--|--|-------------------|

| <p>Adding decimals using column addition</p> | <p>Use place value equipment to represent additions.</p> <p><i>Show $0.23 + 0.45$ using place value counters.</i></p> | <p>Use place value equipment on a place value grid to represent additions.</p> <p>Represent exchange where necessary.</p> <table border="1" style="margin: 10px auto;"> <thead> <tr> <th>O</th> <th>.</th> <th>Tth</th> <th>Hth</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> <td>2 3</td> <td></td> </tr> <tr> <td></td> <td></td> <td>4 5</td> <td></td> </tr> <tr> <td></td> <td></td> <td>6 8</td> <td></td> </tr> </tbody> </table> <p>Include examples where the numbers of decimal places are different.</p> <table border="1" style="margin: 10px auto;"> <thead> <tr> <th>O</th> <th>.</th> <th>Tth</th> <th>Hth</th> </tr> </thead> <tbody> <tr> <td>5</td> <td></td> <td>0</td> <td>0</td> </tr> <tr> <td>1</td> <td></td> <td>2</td> <td>5</td> </tr> <tr> <td>6</td> <td></td> <td>2</td> <td>5</td> </tr> </tbody> </table> | O | . | Tth | Hth | | | 2 3 | | | | 4 5 | | | | 6 8 | | O | . | Tth | Hth | 5 | | 0 | 0 | 1 | | 2 | 5 | 6 | | 2 | 5 | <p>Add using a column method, ensuring that children understand the link with place value.</p> $\begin{array}{r} 0.23 \\ + 0.45 \\ \hline 0.68 \end{array}$ <p>Include exchange where required, alongside an understanding of place value.</p> $\begin{array}{r} 0.92 \\ + 0.33 \\ \hline 1.25 \end{array}$ <p>Include additions where the numbers of decimal places are different.</p> $3.4 + 0.65 = ?$ $\begin{array}{r} 3.40 \\ + 0.65 \\ \hline \end{array}$ |
|---|--|--|-----|---|-----|-----|--|--|-----|--|--|--|-----|--|--|--|-----|--|---|---|-----|-----|---|--|---|---|---|--|---|---|---|--|---|---|--|
| O | . | Tth | Hth | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | 2 3 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | 4 5 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | 6 8 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| O | . | Tth | Hth | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 5 | | 0 | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | | 2 | 5 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 6 | | 2 | 5 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

**Year 5
Subtraction**

| | | | |
|---|--|---|---|
| <p>Column subtraction with whole numbers</p> | <p>Use place value equipment to understand where exchanges are required.</p> <p>$2,250 - 1,070$</p> | <p>Represent the stages of the calculation using place value equipment on a grid alongside the calculation, including exchanges where required.</p> | <p>Use column subtraction methods with exchange where required.</p> |
|---|--|---|---|



$$15,735 - 2,582 = 13,153$$

| TTh | Th | H | T | O | TTh | Th | H | T | O |
|-----|-------|-------|-------|-------|-----|----|---|---|---|
| ● | ●●●●● | ●●●●● | ●●●●● | ●●●●● | 1 | 5 | 7 | 3 | 5 |
| | | ●● | | ●●●● | - | 2 | 5 | 8 | 2 |
| | | | | | | | | | 3 |

Now subtract the 10s. Exchange 1 hundred for 10 tens.

| TTh | Th | H | T | O | TTh | Th | H | T | O |
|-----|-------|-------|-------|-------|-----|----|---|---|---|
| ● | ●●●●● | ●●●●● | ●●●●● | ●●●●● | 1 | 5 | 7 | 3 | 5 |
| | | ●● | ●●●●● | ●●●●● | - | 2 | 5 | 8 | 2 |
| | | | ●●●● | | | | | | 3 |

Subtract the 100s, 1,000s and 10,000s.

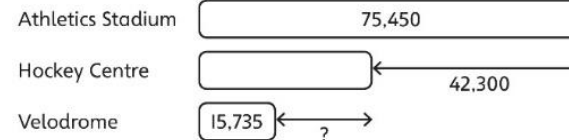
| TTh | Th | H | T | O | TTh | Th | H | T | O | |
|-----|-------|-------|-------|-------|-----|----|---|---|---|---|
| ● | ●●●●● | ●●●●● | ●●●●● | ●●●●● | 1 | 5 | 7 | 3 | 5 | |
| | ●●●● | ●●●● | ●●●● | ●●●● | - | 2 | 5 | 8 | 2 | |
| | | | | | | 1 | 3 | 1 | 5 | 3 |

| TTh | Th | H | T | O |
|----------------|----------------|----------------|---|---|
| 5 8 | 1 2 | 1 0 | 9 | 7 |
| - | 1 | 8 | 5 | 3 |
| | 4 | 3 | 5 | 6 |
| | | | | 3 |

$$62,097 - 18,534 = 43,563$$

Checking strategies and representing subtractions

Bar models represent subtractions in problem contexts, including 'find the difference'.



Children can explain the mistake made when the columns have not been ordered correctly.

| Bella's working | | | | | Correct method | | | | |
|-----------------|----|---|---|---|----------------|----|---|---|---|
| TTh | Th | H | T | O | TTh | Th | H | T | O |
| 1 | 7 | 8 | 7 | 7 | 1 | 7 | 8 | 7 | 7 |
| + | 4 | 0 | 1 | 2 | + | 4 | 0 | 1 | 2 |
| | 5 | 7 | 9 | 9 | | 2 | 1 | 8 | 9 |

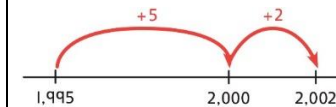
Use approximation to check calculations.

I calculated 18,000 + 4,000 mentally to check my subtraction.

Choosing efficient methods

To subtract two large numbers that are close, children find the difference by counting on.

$$2,002 - 1,995 = ?$$



Use addition to check subtractions.

I calculated 7,546 - 2,355 = 5,191.

I will check using the inverse.

Subtracting decimals

Explore complements to a whole number by working in the context of length.



$$1 \text{ m} - \square \text{ m} = \square \text{ m}$$

$$1 - 0.49 = ?$$

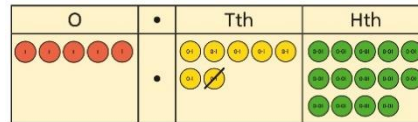
Use a place value grid to represent the stages of column subtraction, including exchanges where required.

$$5.74 - 2.25 = ?$$



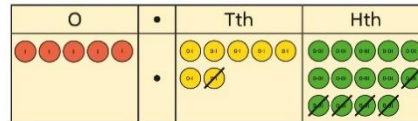
$$\begin{array}{r} \text{O} \cdot \text{Tth} \text{ Hth} \\ 5 \cdot 7 \ 4 \\ - 2 \cdot 2 \ 5 \\ \hline \end{array}$$

Exchange 1 tenth for 10 hundredths.



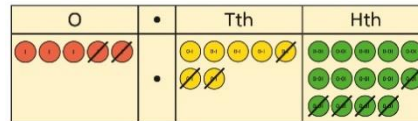
$$\begin{array}{r} \text{O} \cdot \text{Tth} \text{ Hth} \\ 5 \cdot \overset{6}{7} \overset{1}{4} \\ - 2 \cdot 2 \ 5 \\ \hline \end{array}$$

Now subtract the 5 hundredths.



$$\begin{array}{r} \text{O} \cdot \text{Tth} \text{ Hth} \\ 5 \cdot \overset{6}{7} \overset{1}{4} \\ - 2 \cdot 2 \ 5 \\ \hline \cdot \ 9 \end{array}$$

Now subtract the 2 tenths, then the 2 ones.



$$\begin{array}{r} \text{O} \cdot \text{Tth} \text{ Hth} \\ 5 \cdot \overset{6}{7} \overset{1}{4} \\ - 2 \cdot 2 \ 5 \\ \hline 3 \cdot 4 \ 9 \end{array}$$

Use column subtraction, with an understanding of place value, including subtracting numbers with different numbers of decimal places.

$$3.921 - 3.75 = ?$$

$$\begin{array}{r} \text{O} \cdot \text{Tth} \text{ Hth} \text{ Thth} \\ 3 \cdot 9 \ 2 \ 1 \\ - 3 \cdot 7 \ 5 \ 0 \\ \hline \end{array}$$

Year 5 Multiplication

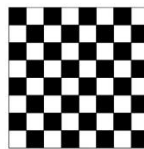
Understanding factors

Use cubes or counters to explore the meaning of 'square numbers'.

25 is a square number because it is made from 5 rows of 5.

Use cubes to explore cube numbers.

Use images to explore examples and non-examples of square numbers.

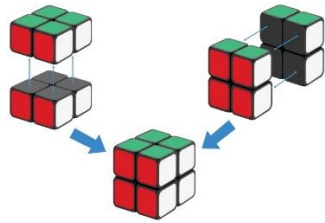


$$8 \times 8 = 64$$

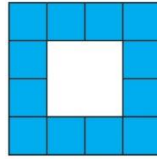
$$8^2 = 64$$

Understand the pattern of square numbers in the multiplication tables.

Use a multiplication grid to circle each square number. Can children spot a pattern?



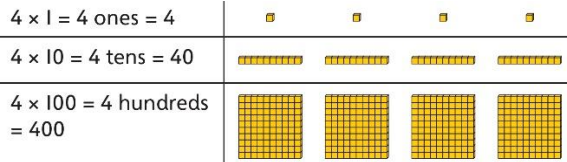
8 is a cube number.



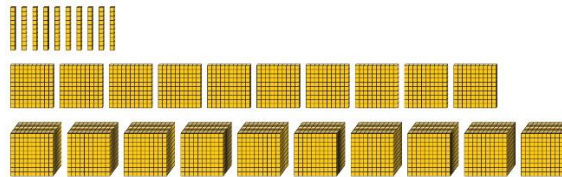
12 is not a square number, because you cannot multiply a whole number by itself to make 12.

Multiplying by 10, 100 and 1,000

Use place value equipment to multiply by 10, 100 and 1,000 by unitising.



Understand the effect of repeated multiplication by 10.



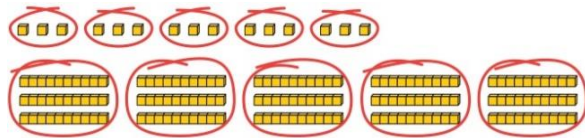
Understand how exchange relates to the digits when multiplying by 10, 100 and 1,000.

| H | T | O |
|---|---|---|
| | 1 | 7 |

$17 \times 10 = 170$
 $17 \times 100 = 17 \times 10 \times 10 = 1,700$
 $17 \times 1,000 = 17 \times 10 \times 10 \times 10 = 17,000$

Multiplying by multiples of 10, 100 and 1,000

Use place value equipment to explore multiplying by unitising.



5 groups of 3 ones is 15 ones.
5 groups of 3 tens is 15 tens.

So, I know that 5 groups of 3 thousands would be 15 thousands.

Use place value equipment to represent how to multiply by multiples of 10, 100 and 1,000.



$4 \times 3 = 12$
 $4 \times 300 = 1,200$
 $6 \times 4 = 24$
 $6 \times 400 = 2,400$

Use known facts and unitising to multiply.

$5 \times 4 = 20$
 $5 \times 40 = 200$
 $5 \times 400 = 2,000$
 $5 \times 4,000 = 20,000$
 $5,000 \times 4 = 20,000$

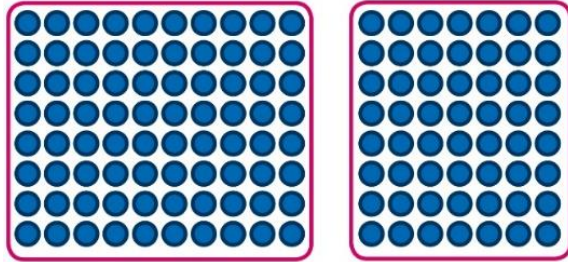
Multiplying up to 4-digit numbers by a single digit

Explore how to use partitioning to multiply efficiently.

$8 \times 17 = ?$

Represent multiplications using place value equipment and add the 1s, then 10s, then 100s, then 1,000s.

Use an area model and then add the parts.



$$8 \times 10 = 80$$

$$8 \times 7 = 56$$

$$80 + 56 = 136$$

So, $8 \times 17 = 136$

| | H | T | O |
|-----|---|----------------|-------|
| 100 | | 10 10 10 10 10 | 1 1 1 |
| 100 | | 10 | |
| 100 | | 10 10 10 10 10 | 1 1 1 |
| 100 | | 10 | |
| 100 | | 10 10 10 10 10 | 1 1 1 |
| 100 | | 10 | |

| | 100 | 60 | 3 |
|---|----------------------|---------------------|-------------------|
| 5 | $100 \times 5 = 500$ | $60 \times 5 = 300$ | $3 \times 5 = 15$ |

Use a column multiplication, including any required exchanges.

$$\begin{array}{r} 136 \\ \times \quad 6 \\ \hline 816 \\ \underline{23} \end{array}$$

Multiplying 2-digit numbers by 2-digit numbers

Partition one number into 10s and 1s, then add the parts.

$$23 \times 15 = ?$$



$$10 \times 15 = 150$$



$$10 \times 15 = 150$$



$$3 \times 15 = 45$$

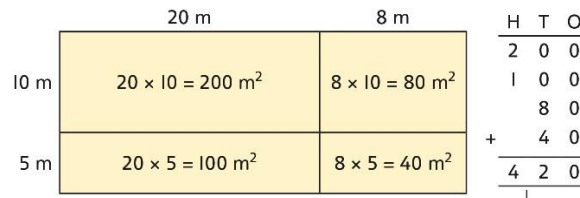
There are 345 bottles of milk in total.

$$\begin{array}{r} \text{H T O} \\ 150 \\ 150 \\ + 45 \\ \hline 345 \end{array}$$

$$23 \times 15 = 345$$

Use an area model and add the parts.

$$28 \times 15 = ?$$



$$28 \times 15 = 420$$

Use column multiplication, ensuring understanding of place value at each stage.

$$\begin{array}{r} 34 \\ \times 27 \\ \hline 238 \end{array} \quad 34 \times 7$$

$$\begin{array}{r} 34 \\ \times 27 \\ \hline 238 \\ 680 \end{array} \quad \begin{array}{l} 34 \times 7 \\ 34 \times 20 \end{array}$$

$$\begin{array}{r} 34 \\ \times 27 \\ \hline 238 \\ 680 \\ 918 \end{array} \quad \begin{array}{l} 34 \times 7 \\ 34 \times 20 \\ 34 \times 27 \end{array}$$

Multiplying up to 4-digits by 2-digits

Use the area model then add the parts.

Use column multiplication, ensuring understanding of place value at each stage.

| | 100 | 40 | 3 |
|----|-----|----|---|
| 10 | | | |
| 2 | | | |

$$143 \times 12 = 1,716$$

There are 1,716 boxes of cereal in total.

$$143 \times 12 = 1,716$$

| | Th | H | T | O |
|---|----|---|---|---|
| | 1 | 0 | 0 | 0 |
| | | 4 | 0 | 0 |
| | | 2 | 0 | 0 |
| | | | 8 | 0 |
| | | | 3 | 0 |
| + | | | | 6 |
| | 1 | 7 | 1 | 6 |

| | | | | |
|---|---|---|---|---------|
| | 1 | 4 | 3 | |
| x | | 1 | 2 | |
| | 2 | 8 | 6 | 143 × 2 |
| | 1 | 4 | 3 | 0 |
| | 1 | 7 | 1 | 6 |

143 × 10
143 × 12

Progress to include examples that require multiple exchanges as understanding, confidence and fluency build.

$$1,274 \times 32 = ?$$

First multiply 1,274 by 2.

| | | | | | |
|---|---|---|---|---|-----------|
| | 1 | 2 | 7 | 4 | |
| x | | | 3 | 2 | |
| | 2 | 5 | 4 | 8 | 1,274 × 2 |

Then multiply 1,274 by 30.

| | | | | | |
|---|---|---|---|---|------------|
| | 1 | 2 | 7 | 4 | |
| x | | | 3 | 2 | |
| | 2 | 5 | 4 | 8 | 1,274 × 2 |
| | 3 | 8 | 2 | 2 | 0 |
| | | | | | 1,274 × 30 |

Finally, find the total.

| | | | | | |
|---|---|---|---|---|-----------|
| | 1 | 2 | 7 | 4 | |
| x | | | 3 | 2 | |
| | 2 | 5 | 4 | 8 | 1,274 × 2 |
| | 3 | 8 | 2 | 2 | 0 |
| | 4 | 0 | 7 | 6 | 8 |

1,274 × 30
1,274 × 32

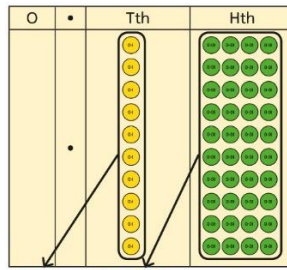
$$1,274 \times 32 = 40,768$$

Multiplying decimals by 10, 100 and 1,000

Use place value equipment to explore and understand the exchange of 10 tenths, 10 hundredths or 10 thousandths.

Represent multiplication by 10 as exchange on a place value grid.

Understand how this exchange is represented on a place value chart.



$$0.14 \times 10 = 1.4$$

| Th | H | T | O | . | Tth |
|----|---|---|---|---|-----|
| | | | 2 | . | 5 |
| | | 2 | 5 | . | |
| 2 | 5 | 0 | 0 | . | |

$$2.5 \times 10 = 25$$

$$2.5 \times 100 = 250$$

$$2.5 \times 1,000 = 2,500$$

Year 5 Division

Understanding factors and prime numbers

Use equipment to explore the factors of a given number.

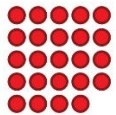


$$24 \div 3 = 8$$

$$24 \div 8 = 3$$

8 and 3 are factors of 24 because they divide 24 exactly.

$$24 \div 5 = 4 \text{ remainder } 4.$$



5 is not a factor of 24 because there is a remainder.

Understand that prime numbers are numbers with exactly two factors.

$$13 \div 1 = 13$$

$$13 \div 2 = 6 \text{ r } 1$$

$$13 \div 4 = 4 \text{ r } 1$$

1 and 13 are the only factors of 13.
13 is a prime number.

Understand how to recognise prime and composite numbers.

I know that 31 is a prime number because it can be divided by only 1 and itself without leaving a remainder.

I know that 33 is not a prime number as it can be divided by 1, 3, 11 and 33.

I know that 1 is not a prime number, as it has only 1 factor.

Understanding inverse operations and the link with multiplication, grouping and sharing

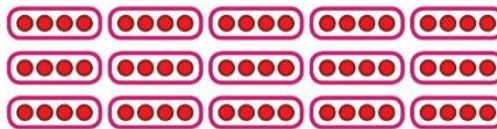
Use equipment to group and share and to explore the calculations that are present.

I have 28 counters.

I made 7 groups of 4. There are 28 in total.

I have 28 in total. I shared them equally into 7 groups. There are 4 in each group.

Represent multiplicative relationships and explore the families of division facts.



$$60 \div 4 = 15$$

$$60 \div 15 = 4$$

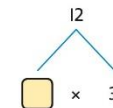
Represent the different multiplicative relationships to solve problems requiring inverse operations.

$$12 \div 3 = \square$$

$$12 \div \square = 3$$

$$\square \times 3 = 12$$

$$\square \div 3 = 12$$



I have 28 in total. I made groups of 4. There are 7 equal groups.

Understand missing number problems for division calculations and know how to solve them using inverse operations.

$$22 \div ? = 2$$

$$22 \div 2 = ?$$

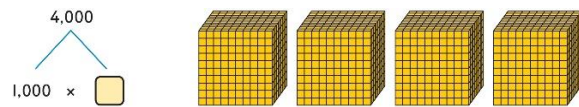
$$? \div 2 = 22$$

$$? \div 22 = 2$$

Dividing whole numbers by 10, 100 and 1,000

Use place value equipment to support unitising for division.

$$4,000 \div 1,000$$



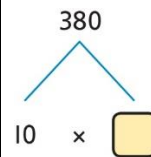
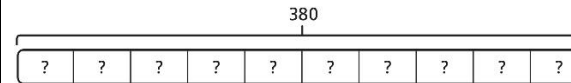
4,000 is 4 thousands.

$$4 \times 1,000 = 4,000$$

So, $4,000 \div 1,000 = 4$

Use a bar model to support dividing by unitising.

$$380 \div 10 = 38$$



380 is 38 tens.

$$38 \times 10 = 380$$

$$10 \times 38 = 380$$

So, $380 \div 10 = 38$

Understand how and why the digits change on a place value grid when dividing by 10, 100 or 1,000.

| Th | H | T | O |
|----|---|---|---|
| 3 | 2 | 0 | 0 |

$$3,200 \div 100 = ?$$

3,200 is 3 thousands and 2 hundreds.

$$200 \div 100 = 2$$

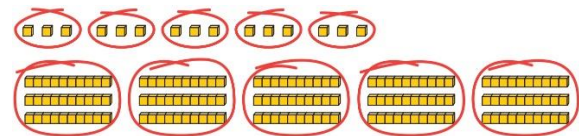
$$3,000 \div 100 = 30$$

$$3,200 \div 100 = 32$$

So, the digits will move two places to the right.

Dividing by multiples of 10, 100 and 1,000

Use place value equipment to represent known facts and unitising.

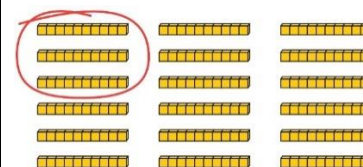


15 ones put into groups of 3 ones. There are 5 groups.

$$15 \div 3 = 5$$

15 tens put into groups of 3 tens. There are 5 groups.

Represent related facts with place value equipment when dividing by unitising.



180 is 18 tens.

18 tens divided into groups of 3 tens. There are 6 groups.

$$180 \div 30 = 6$$

Reason from known facts, based on understanding of unitising. Use knowledge of the inverse relationship to check.

$$3,000 \div 5 = 600$$

$$3,000 \div 50 = 60$$

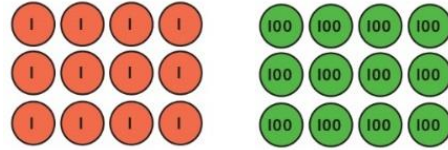
$$3,000 \div 500 = 6$$

$$5 \times 600 = 3,000$$

$$50 \times 60 = 3,000$$

$$500 \times 6 = 3,000$$

$$150 \div 30 = 5$$



12 ones divided into groups of 4. There are 3 groups.

12 hundreds divided into groups of 4 hundreds. There are 3 groups.

$$1200 \div 400 = 3$$

Dividing up to four digits by a single digit using short division

Explore grouping using place value equipment.

$$268 \div 2 = ?$$

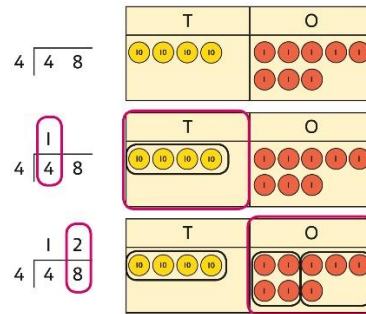
*There is 1 group of 2 hundreds.
There are 3 groups of 2 tens.
There are 4 groups of 2 ones.*

$$264 \div 2 = 134$$

Use place value equipment on a place value grid alongside short division.

The model uses grouping.

A sharing model can also be used, although the model would need adapting.



Lay out the problem as a short division.

*There is 1 group of 4 in 4 tens.
There are 2 groups of 4 in 8 ones.*

Work with divisions that require exchange.

Use short division for up to 4-digit numbers divided by a single digit.

$$\begin{array}{r} 0556 \\ 7 \overline{) 3892} \end{array}$$

$$3,892 \div 7 = 556$$

Use multiplication to check.

$$556 \times 7 = ?$$

$$6 \times 7 = 42$$

$$50 \times 7 = 350$$

$$500 \times 7 = 3500$$

$$3,500 + 350 + 42 = 3,892$$

| | | <div style="display: flex; flex-direction: column; align-items: flex-start;"> <div style="display: flex; align-items: center; margin-bottom: 10px;"> $4 \overline{) 92}$ <div style="margin-left: 10px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><th>T</th><th>O</th></tr> <tr><td>10 10 10 10</td><td>2 2</td></tr> </table> </div> <div style="margin-left: 10px;">First, lay out the problem.</div> </div> <div style="display: flex; align-items: center; margin-bottom: 10px;"> $4 \overline{) 92}$ <div style="margin-left: 10px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><th>T</th><th>O</th></tr> <tr><td>10 10 10 10</td><td>2 2</td></tr> </table> </div> <div style="margin-left: 10px;">How many groups of 4 go into 9 tens?</div> </div> <div style="display: flex; align-items: center; margin-bottom: 10px;"> $4 \overline{) 92}$ <div style="margin-left: 10px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><th>T</th><th>O</th></tr> <tr><td>10 10 10 10</td><td>2 2</td></tr> </table> </div> <div style="margin-left: 10px;">2 groups of 4 tens with 1 ten left over.</div> </div> <div style="display: flex; align-items: center; margin-bottom: 10px;"> $4 \overline{) 92}$ <div style="margin-left: 10px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><th>T</th><th>O</th></tr> <tr><td>10 10 10 10</td><td>2 2</td></tr> </table> </div> <div style="margin-left: 10px;">Exchange the 1 ten left over for 10 ones.</div> </div> <div style="display: flex; align-items: center; margin-bottom: 10px;"> $4 \overline{) 92}$ <div style="margin-left: 10px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><th>T</th><th>O</th></tr> <tr><td>10 10 10 10</td><td>2 2</td></tr> </table> </div> <div style="margin-left: 10px;">We now have 12 ones.</div> </div> <div style="display: flex; align-items: center;"> $4 \overline{) 92}$ <div style="margin-left: 10px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><th>T</th><th>O</th></tr> <tr><td>10 10 10 10</td><td>2 2</td></tr> </table> </div> <div style="margin-left: 10px;">How many groups of 4 go into 12 ones?</div> </div> <div style="margin-left: 10px;">3 groups of 4 ones.</div> </div> | T | O | 10 10 10 10 | 2 2 | T | O | 10 10 10 10 | 2 2 | T | O | 10 10 10 10 | 2 2 | T | O | 10 10 10 10 | 2 2 | T | O | 10 10 10 10 | 2 2 | T | O | 10 10 10 10 | 2 2 |
|-------------|-----|--|---|---|-------------|-----|---|---|-------------|-----|---|---|-------------|-----|---|---|-------------|-----|---|---|-------------|-----|---|---|-------------|-----|
| T | O | | | | | | | | | | | | | | | | | | | | | | | | | |
| 10 10 10 10 | 2 2 | | | | | | | | | | | | | | | | | | | | | | | | | |
| T | O | | | | | | | | | | | | | | | | | | | | | | | | | |
| 10 10 10 10 | 2 2 | | | | | | | | | | | | | | | | | | | | | | | | | |
| T | O | | | | | | | | | | | | | | | | | | | | | | | | | |
| 10 10 10 10 | 2 2 | | | | | | | | | | | | | | | | | | | | | | | | | |
| T | O | | | | | | | | | | | | | | | | | | | | | | | | | |
| 10 10 10 10 | 2 2 | | | | | | | | | | | | | | | | | | | | | | | | | |
| T | O | | | | | | | | | | | | | | | | | | | | | | | | | |
| 10 10 10 10 | 2 2 | | | | | | | | | | | | | | | | | | | | | | | | | |
| T | O | | | | | | | | | | | | | | | | | | | | | | | | | |
| 10 10 10 10 | 2 2 | | | | | | | | | | | | | | | | | | | | | | | | | |

Year 6

Concrete

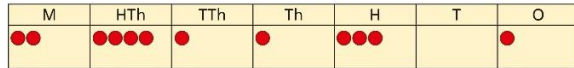
Pictorial

Abstract

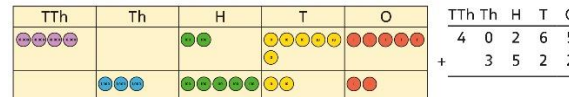
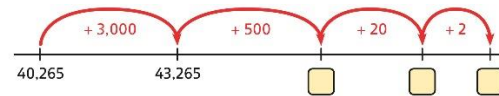
Year 6 Addition

Comparing and selecting efficient methods

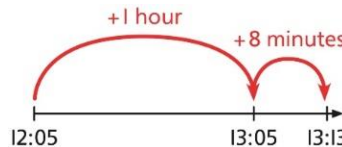
Represent 7-digit numbers on a place value grid, and use this to support thinking and mental methods.



Discuss similarities and differences between methods, and choose efficient methods based on the specific calculation. Compare written and mental methods alongside place value representations.

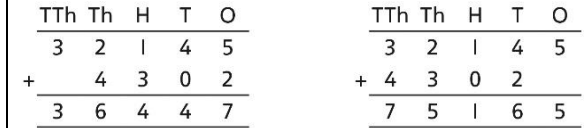


Use bar model and number line representations to model addition in problem-solving and measure contexts.



Use column addition where mental methods are not efficient. Recognise common errors with column addition.

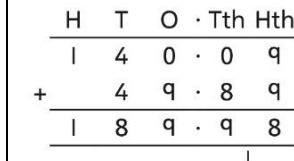
$32,145 + 4,302 = ?$



Which method has been completed accurately?

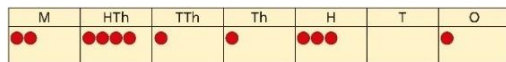
What mistake has been made?

Column methods are also used for decimal additions where mental methods are not efficient.



Selecting mental methods for larger numbers where appropriate

Represent 7-digit numbers on a place value grid, and use this to support thinking and mental methods.



Use a bar model to support thinking in addition problems.

$257,000 + 99,000 = ?$

Use place value and unitising to support mental calculations with larger numbers.

$195,000 + 6,000 = ?$

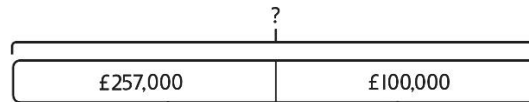
$195 + 5 + 1 = 201$

$$2,411,301 + 500,000 = ?$$

This would be 5 more counters in the HTh place.

So, the total is 2,911,301.

$$2,411,301 + 500,000 = 2,911,301$$



I added 100 thousands then subtracted 1 thousand.

257 thousands + 100 thousands = 357 thousands

$$257,000 + 100,000 = 357,000$$

$$357,000 - 1,000 = 356,000$$

So, $257,000 + 99,000 = 356,000$

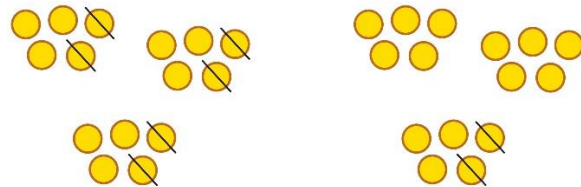
195 thousands + 6 thousands = 201 thousands

$$\text{So, } 195,000 + 6,000 = 201,000$$

Understanding order of operations in calculations

Use equipment to model different interpretations of a calculation with more than one operation. Explore different results.

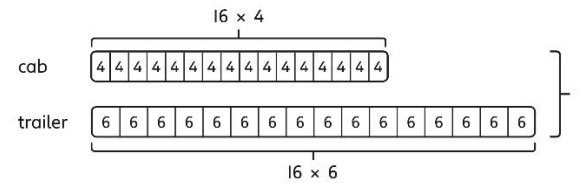
$$3 \times 5 - 2 = ?$$



$$\begin{array}{l} 3 \times (5 - 2) \\ \downarrow \quad \downarrow \\ 3 \times 3 = 9 \end{array}$$

$$\begin{array}{l} (3 \times 5) - 2 \\ \downarrow \quad \downarrow \\ 15 - 2 = 13 \end{array}$$

Model calculations using a bar model to demonstrate the correct order of operations in multi-step calculations.



This can be written as: $16 \times 4 + 16 \times 6$
 $64 + 96 = 160$

Understand the correct order of operations in calculations without brackets.

Understand how brackets affect the order of operations in a calculation.

$$\begin{array}{l} 4 + 6 \times 16 \\ 4 + 96 = 100 \end{array}$$

$$\begin{array}{l} (4 + 6) \times 16 \\ 10 \times 16 = 160 \end{array}$$

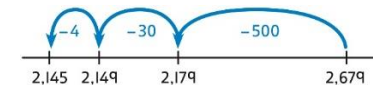
Year 6 Subtraction

Comparing and selecting efficient methods

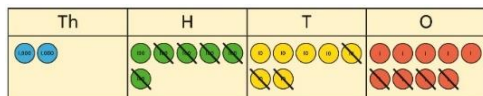
Use counters on a place value grid to represent subtractions of larger numbers.



Compare subtraction methods alongside place value representations.

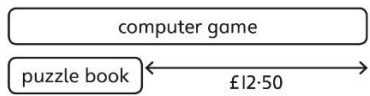


Compare and select methods. Use column subtraction when mental methods are not efficient. Use two different methods for one calculation as a checking strategy.

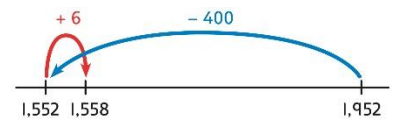


$$\begin{array}{r}
 \text{Th H T O} \\
 2\ 6\ 7\ 9 \\
 -\ 5\ 3\ 4 \\
 \hline
 2\ 1\ 4\ 5
 \end{array}$$

Use a bar model to represent calculations, including 'find the difference' with two bars as comparison.



| Th | H | T | O |
|----|---|----|---|
| 1 | 8 | 14 | 2 |
| - | 1 | 5 | 5 |
| 3 | 9 | 4 | |



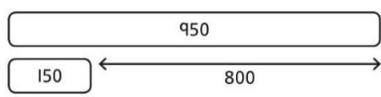
Use column subtraction for decimal problems, including in the context of measure.

$$\begin{array}{r}
 \text{H T O} \cdot \text{Tth Hth} \\
 3\ 0\ 9 \cdot 6\ 0 \\
 -\ 2\ 0\ 6 \cdot 4\ 0 \\
 \hline
 1\ 0\ 3 \cdot 2\ 0
 \end{array}$$

Subtracting mentally with larger numbers

Use a bar model to show how unitising can support mental calculations.

$950,000 - 150,000$
That is 950 thousands - 150 thousands



So, the difference is 800 thousands.
 $950,000 - 150,000 = 800,000$

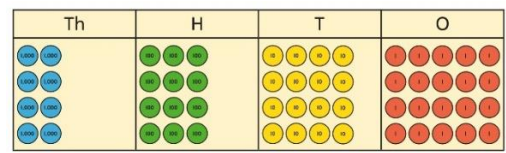
Subtract efficiently from powers of 10.

$10,000 - 500 = ?$

Year 6 Multiplication

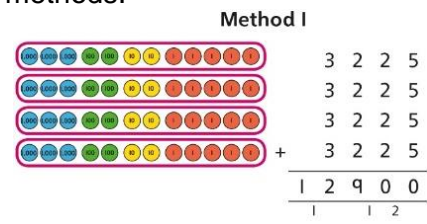
Multiplying up to a 4-digit number by a single digit number

Use equipment to explore multiplications.



4 groups of 2,345

Use place value equipment to compare methods.



Understand area model and short multiplication.

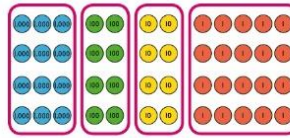
Compare and select appropriate methods for specific multiplications.

This is a multiplication:

$$4 \times 2,345$$

$$2,345 \times 4$$

Method 2



$$4 \times 3,000 \quad 4 \times 200 \quad 4 \times 20 \quad 4 \times 5$$

$$12,000 + 800 + 80 + 20 = 12,900$$

Method 3

| | | | | |
|---|--------|-----|----|----|
| | 3,000 | 200 | 20 | 5 |
| 4 | 12,000 | 800 | 80 | 20 |

$$12,000 + 800 + 80 + 20 = 12,900$$

Method 4

$$\begin{array}{r} 3 \ 2 \ 2 \ 5 \\ \times \quad \quad 4 \\ \hline 1 \ 2 \ 9 \ 0 \ 0 \\ \hline \quad \quad \quad 1 \ 2 \end{array}$$

Multiplying up to a 4-digit number by a 2-digit number

Use an area model alongside written multiplication.

Method 1

| | | | | |
|----|--------|-------|-----|-----|
| | 1,000 | 200 | 30 | 5 |
| 20 | 20,000 | 4,000 | 600 | 100 |
| 1 | 1,000 | 200 | 30 | 5 |

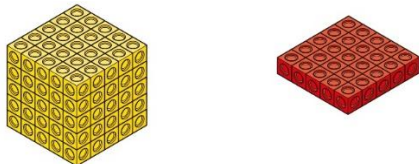
$$\begin{array}{r} 1 \ 2 \ 3 \ 5 \\ \times \quad \quad 2 \ 1 \\ \hline \quad \quad \quad 5 \quad 1 \times 5 \\ \quad \quad 3 \ 0 \quad 1 \times 30 \\ \quad 2 \ 0 \ 0 \quad 1 \times 200 \\ 1 \ 0 \ 0 \ 0 \quad 1 \times 1,000 \\ 1 \ 0 \ 0 \quad 20 \times 5 \\ 6 \ 0 \ 0 \quad 20 \times 30 \\ 4 \ 0 \ 0 \ 0 \quad 20 \times 200 \\ 2 \ 0 \ 0 \ 0 \ 0 \quad 20 \times 1,000 \\ \hline 2 \ 5 \ 9 \ 3 \ 5 \quad 21 \times 1,235 \end{array}$$

Use compact column multiplication with understanding of place value at all stages.

$$\begin{array}{r} 1 \ 2 \ 3 \ 5 \\ \times \quad \quad 2 \ 1 \\ \hline 1 \ 2 \ 3 \ 5 \quad 1 \times 1,235 \\ 2 \ 4 \ 7 \ 0 \ 0 \quad 20 \times 1,235 \\ \hline 2 \ 5 \ 9 \ 3 \ 5 \quad 21 \times 1,235 \end{array}$$

Using knowledge of factors and partitions to compare methods for multiplications

Use equipment to understand square numbers and cube numbers.

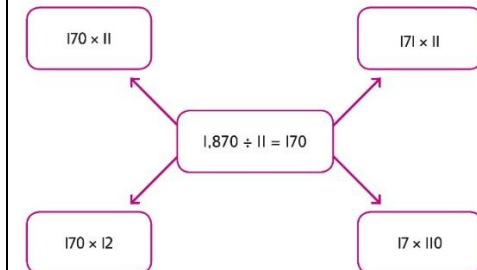


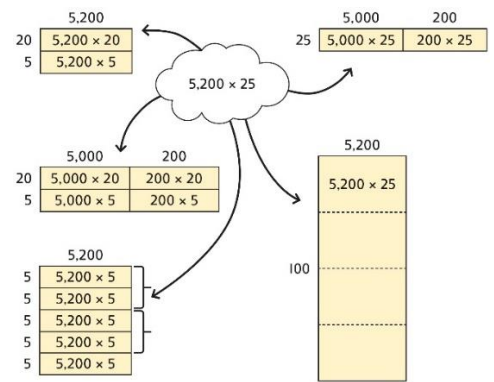
$$5 \times 5 = 5^2 = 25$$

$$5 \times 5 \times 5 = 5^3 = 25 \times 5 = 125$$

Compare methods visually using an area model. Understand that multiple approaches will produce the same answer if completed accurately.

Use a known fact to generate families of related facts.





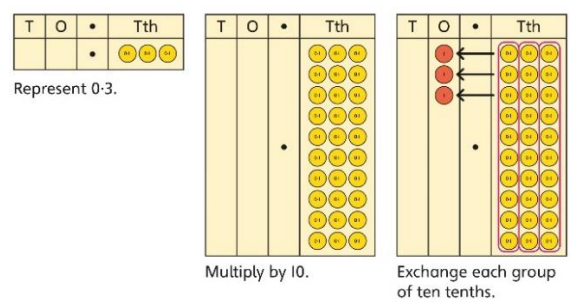
Represent and compare methods using a bar model.

Use factors to calculate efficiently.

$$\begin{aligned}
 15 \times 16 &= 3 \times 5 \times 2 \times 8 \\
 &= 3 \times 8 \times 2 \times 5 \\
 &= 24 \times 10 \\
 &= 240
 \end{aligned}$$

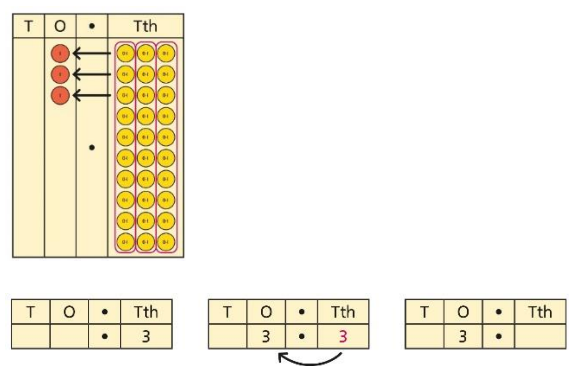
Multiplying by 10, 100 and 1,000

Use place value equipment to explore exchange in decimal multiplication.



$0.3 \times 10 = ?$
 0.3 is 3 tenths.
 10 x 3 tenths are 30 tenths.
 30 tenths are equivalent to 3 ones.

Understand how the exchange affects decimal numbers on a place value grid.



$$0.3 \times 10 = 3$$

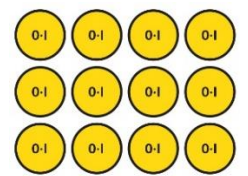
Use knowledge of multiplying by 10, 100 and 1,000 to multiply by multiples of 10, 100 and 1,000.

$$\begin{aligned}
 8 \times 100 &= 800 \\
 8 \times 300 &= 800 \times 3 \\
 &= 2,400
 \end{aligned}$$

$$\begin{aligned}
 2.5 \times 10 &= 25 \\
 2.5 \times 20 &= 2.5 \times 10 \times 2 \\
 &= 50
 \end{aligned}$$

Multiplying decimals

Explore decimal multiplications using place value equipment and in the context of measures.



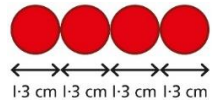
Represent calculations on a place value grid.

Use known facts to multiply decimals.

$$\begin{aligned}
 4 \times 3 &= 12 \\
 4 \times 0.3 &= 1.2 \\
 4 \times 0.03 &= 0.12
 \end{aligned}$$

$$\begin{aligned}
 20 \times 5 &= 100 \\
 20 \times 0.5 &= 10 \\
 20 \times 0.05 &= 1
 \end{aligned}$$

3 groups of 4 tenths is 12 tenths.
4 groups of 3 tenths is 12 tenths.



$$4 \times 1 \text{ cm} = 4 \text{ cm}$$

$$4 \times 0.3 \text{ cm} = 1.2 \text{ cm}$$

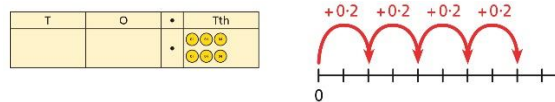
$$4 \times 1.3 = 4 + 1.2 = 5.2 \text{ cm}$$

$$3 \times 3 = 9$$

$$3 \times 0.3 = 0.9$$

| T | O | • | Tth |
|---|---|---|-------------|
| | | | 0.1 0.1 0.1 |
| | | | 0.1 0.1 0.1 |
| | | | 0.1 0.1 0.1 |

Understand the link between multiplying decimals and repeated addition.



Find families of facts from a known multiplication.

I know that $18 \times 4 = 72$.

This can help me work out:

$$1.8 \times 4 = ?$$

$$18 \times 0.4 = ?$$

$$180 \times 0.4 = ?$$

$$18 \times 0.04 = ?$$

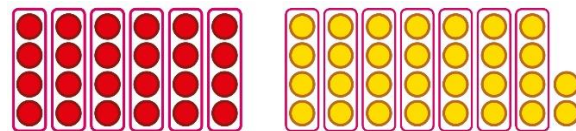
Use a place value grid to understand the effects of multiplying decimals.

| | H | T | O | • | Tth | Hth |
|-----------------|---|---|---|---|-----|-----|
| 2×3 | | | 6 | • | | |
| 0.2×3 | | | 0 | • | 6 | |
| 0.02×3 | | | | • | | |

Year 6 Division

Understanding factors

Use equipment to explore different factors of a number.

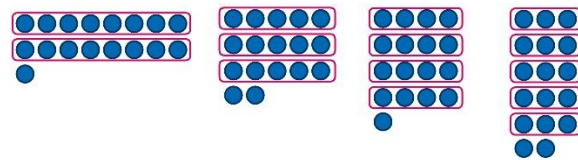


$$24 \div 4 = 6$$

$$30 \div 4 = 7 \text{ remainder } 2$$

4 is a factor of 24 but is not a factor of 30.

Recognise prime numbers as numbers having exactly two factors. Understand the link with division and remainders.



$$17 \div 2 = 8 \text{ r } 1$$

$$17 \div 3 = 5 \text{ r } 2$$

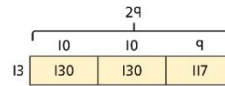
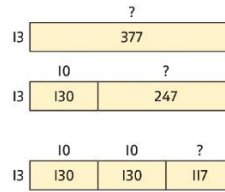
$$17 \div 4 = 4 \text{ r } 1$$

$$17 \div 5 = 3 \text{ r } 2$$

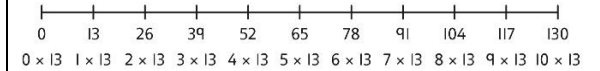
Recognise and know primes up to 100. Understand that 2 is the only even prime, and that 1 is not a prime number.

| | | | | | | | | | |
|----|----|----|----|----|----|----|----|----|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |

182 divided into groups of 13.
There are 14 groups.



$$377 \div 13 = 29$$



$$\begin{array}{r} 13 \overline{) 377} \\ - 130 \quad 10 \\ \hline 247 \\ - 130 \quad 10 \\ \hline 117 \\ - 117 \quad 9 \\ \hline 0 \quad 29 \end{array}$$

$$377 \div 13 = 29$$

A slightly different layout may be used, with the division completed above rather than at the side.

$$\begin{array}{r} 3 \\ 21 \overline{) 798} \\ - 630 \\ \hline 168 \end{array}$$

$$\begin{array}{r} 38 \\ 21 \overline{) 798} \\ - 630 \\ \hline 168 \\ - 168 \\ \hline 0 \end{array}$$

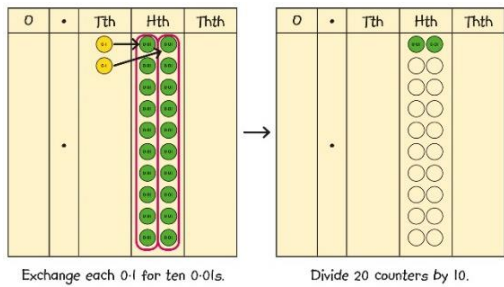
Divisions with a remainder explored in problem-solving contexts.

Dividing by 10, 100 and 1,000

Use place value equipment to explore division as exchange.

Represent division to show the relationship with multiplication. Understand the effect of dividing by 10, 100 and 1,000 on the digits on a place value grid.

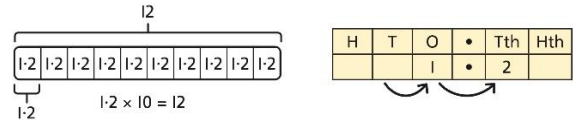
Use knowledge of factors to divide by multiples of 10, 100 and 1,000.



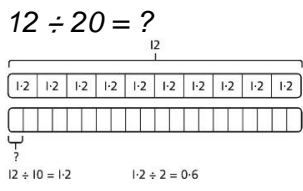
Exchange each 0.1 for ten 0.01s.

Divide 20 counters by 10.

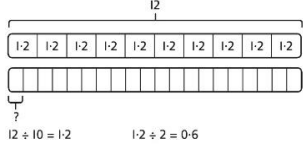
0.2 is 2 tenths.
 2 tenths is equivalent to 20 hundredths.
 20 hundredths divided by 10 is 2 hundredths.



Understand how to divide using division by 10, 100 and 1,000.

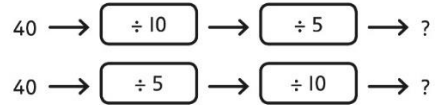


$12 \div 20 = ?$



$12 \div 2 = 0.6$

$40 \div 50 = \square$

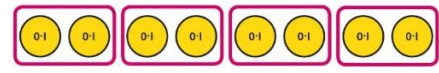


$40 \div 5 = 8$
 $8 \div 10 = 0.8$

So, $40 \div 50 = 0.8$

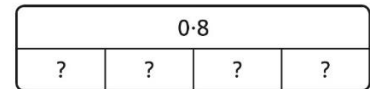
Dividing decimals

Use place value equipment to explore division of decimals.



8 tenths divided into 4 groups. 2 tenths in each group.

Use a bar model to represent divisions.



$4 \times 2 = 8$ $8 \div 4 = 2$
 So, $4 \times 0.2 = 0.8$ $0.8 \div 4 = 0.2$

Use short division to divide decimals with up to 2 decimal places.

